

Computing pseudo inverse

- We want matrix multiplication to get as close to \mathbf{I} as possible. Consider the 3×4 diagonal matrix:

$$\begin{bmatrix} 1/a & 0 & 0 \\ 0 & 1/b & 0 \\ 0 & 0 & 0 \end{bmatrix} \times \begin{bmatrix} a & 0 & 0 & 0 \\ 0 & b & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

- For an $n \times n$ diagonal matrix $\mathbf{\Sigma}$, $\mathbf{\Sigma}^+ = \mathbf{\Sigma}^{-1}$
- For any invertible $n \times n$ matrix \mathbf{X} , $\mathbf{X}^+ = \mathbf{X}^{-1}$
- In general, if we use singular value decomposition $\mathbf{X}^+ = \mathbf{V}\mathbf{\Sigma}^+\mathbf{U}^T$

Summary / next

- We reviewed SVD and pseudo inverse
- SVD is a very important method. We will return to it multiple times during the course

Next:

- A very short introduction to calculus

the SVD song

Further reading

Any of the linear algebra references provided earlier.